

Unit 3 Study Guide B

Factoring and Solving Quadratic Equations: MGSE9-12.A.REI.4 & MGSE9-12.A.REI.4b

Remember to show work!

Use factoring and the Zero-Product Property to find the zeros (solutions) of the quadratic equations.

1. $x^2 - 14x - 15 = 0$

$$(x-15)(x+1) = 0$$

$$\boxed{\{-1, 15\}}$$

2. $3x^2 + 2x - 8 = 0$

$$x^2 + 2x - 24$$

$$(x+\frac{6}{3})(x-\frac{4}{3})$$

$$\boxed{\{-2, \frac{4}{3}\}}$$

3. $5x^2 + 4x - 12 = 0$

$$x^2 + 4x - 60 = 0$$

$$(x+10)(x-6) = 0$$

$$\boxed{\{-2, \frac{6}{5}\}}$$

4. $2x^2 - 50 = 0$

$$2(x^2 - 25) = 0$$

$$\boxed{\{\pm 5\}}$$

5. $x^2 + 3x - 10 = 0$

$$(x+5)(x-2) = 0$$

$$\boxed{\{-5, 2\}}$$

6. $5x^2 + 10x + 5 = 0$

$$5(x^2 + 2x + 1) = 0$$

$$\boxed{\{-1\}}$$

Solve each equation by using square roots.

7. $\frac{3x^2}{3} = \frac{27}{3}$

$$x^2 = 9$$

$$x = \pm 3$$

8. $(x+8)^2 = 32$

$$x+8 = \pm \sqrt{32}$$

$$x+8 = \pm 4\sqrt{2}$$

$$x = -8 \pm 4\sqrt{2}$$

9. $3(x-2)^2 + 4 = 52$

$$\underline{\underline{\frac{3(x-2)^2}{3} = \frac{48}{3}}}$$

$$(x-2)^2 = 16$$

$$x-2 = 4$$

$$x = 6$$

$$x-2 = -4$$

$$x = -2$$

$$\boxed{\{-2, 6\}}$$

Solve each equation by completing the square.

10. $x^2 - 6x + 5 = 0$

$$\begin{aligned} & (x-3)^2 = 4 \\ & x-3 = \pm 2 \\ & x = 5 \quad x = 1 \end{aligned}$$

11. $-12x = 3x^2 - 9$

$$\begin{aligned} & 3x^2 + 12x - 9 = 0 \\ & 3(x^2 + 4x - 3) = 0 \\ & x^2 + 4x + 4 = 3 + 4 \\ & (x+2)^2 = 7 \\ & x = -2 \pm \sqrt{7} \end{aligned}$$

Use the quadratic formula to solve the equations.

12. $-7x^2 - 5x + 1 = 0$

$$\begin{aligned} & \frac{-(-5) \pm \sqrt{(-5)^2 - 4(-7)(1)}}{2(-7)} \\ & \frac{5 \pm \sqrt{53}}{-14} \end{aligned}$$

13. $x^2 - 4x - 12 = 0$

$$\begin{aligned} & \frac{-(-4) \pm \sqrt{(-4)^2 - 4(1)(-12)}}{2(1)} \\ & \frac{4 \pm \sqrt{64}}{2} = \frac{4 \pm 8}{2} \\ & \{6, -2\} \end{aligned}$$

14. $x^2 - 5x + 6 = 0$

$$x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(1)(6)}}{2(1)} = \frac{5 \pm \sqrt{1}}{2}$$

$$\begin{aligned} & \frac{5 \pm 1}{2} \\ & \frac{5+1}{2} \quad \frac{5-1}{2} \\ & \{3, 2\} \end{aligned}$$

Error Analysis: Find and circle the error. Then give the correct answer.

15. Solve the equation by completing the square.

$$x^2 - 8x + 12 = 0$$

$$x^2 - 8x = -12$$

$$x^2 - 8x + 16 = -12 + 16$$

$$(x-4)^2 = 28 - 4$$

$$x-4 = \sqrt{28}$$

$$x = 4 \pm 2\sqrt{7}$$

$$\begin{aligned} & x^2 - 8x = -12 \\ & x^2 - 8x + 16 = -12 + 16 \\ & (x-4)^2 = 4 \\ & x-4 = \pm 2 \\ & x = 6 \quad x = 2 \end{aligned}$$

$$\{2, 6\}$$